

MATH 100, Tutorial 8

(Week of March 11, 2024)

Exercise 1. Find $f'(x)$ for the following functions:

$$(a) f(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}.$$

$$(b) f(x) = e^x \ln x.$$

$$(c) f(x) = \frac{e^{-x}}{x}.$$

$$(d) f(x) = \sqrt{e^{3x} + 4x}.$$

$$(e) f(x) = x^\pi \cdot \pi^x$$

$$(f) f(x) = \ln(5x^3 + 2x).$$

$$(g) f(x) = 3^{\sin 3x}.$$

$$(h) f(x) = 3^{9x} + 9x^2.$$

$$(i) f(x) = \log_7(6x^4 + 3)^5.$$

Exercise 2. Use logarithmic differentiation to find y' (that is $\frac{dy}{dx}$).

$$(a) y = (\cos 2x)^{4x}.$$

$$(b) y = (2x)^{\sqrt{2x}}.$$

$$(c) y = (\ln x)^{\ln x}.$$

$$(d) y = (x^3 - 1)^{\ln x}.$$

$$(e) y = x^{-1/2}(x^2 + 5)^{2/3}(2x - 3)^5.$$